

## Key Design Features

- Synthesizable, technology independent VHDL Core
- Half-band polyphase decimation filter with a configurable decimation factor from 2 to 2<sup>N</sup>
- FIR filter core implemented as an optimized 48-tap systolic array (24-taps per phase) for ultimate speed and minimal resource use
- Configurable data and coefficient widths
- Symmetric arithmetic rounding limits DC-bias problems
- Saturation of output samples no wrap
- Ships with 14-bit coefficients giving 80 dB stop-band attenuation
- Only 12 H/W multipliers used per decimate-by-2 stage
- Supports input sample rates of up to 300 MHz+

## Applications

- Decimation of signals after digital-down-conversion
- Decimation by a wide range of factors from 2 to 2<sup>N</sup>
- Reduction of input sample rate to make subsequent signal processing easier

# **Generic Parameters**

Generic name	Description	Туре	Valid range
num_stages	Number of decimate- by-2 filter stages (N)	integer	≥ 1
dw	Width of input/output data samples	integer	≥2
cw	Width of coefficients	integer	≥ 2
fw	Number of coefficient fraction bits	integer	≥ 0 (fw < cw)

## **Pin-out Description**

Pin name	I/O	Description	Active state
clk	in	System clock (Fs)	rising edge
reset	in	System reset	low
en	in	Clock enable in	high
en_out	out	Clock enable out	high
x_in	in	Input samples (signed number)	data
y_out	out	Decimated output samples (signed number)	data



Figure 1: Decimation Filter Architecture

### **General Description**

Block Diagram

FIR\_DEC\_N is a polyphase decimation filter that permits the downsampling of an input signal by any power of 2. The filter core is organized as a highly optimized systolic array, allowing the user to specify very large decimation factors while keeping resource costs to a minimum.

Input data is sampled on the rising clock-edge of clk when en is active high. Internally, the samples are filtered and decimated then presented at the output interface,  $y_out$ .

The output signal *en\_out* is the output clock-enable signal that indicates when an output sample is valid. For instance, when decimating by a factor of 2, then *en\_out* will have a duty cycle of 50% relative to the input clock-enable signal. When decimating by a factor of 4, the duty cycle will be 25% and so on.

#### Filter coefficients and I/O specification

Filter coefficients<sup>1</sup> are defined as signed fixed-point numbers in [cw fw] format where cw is the total number of coefficient bits and fw is the number of bits in the fractional part. In all cases, cw must be at least 2 bits and fw must be less than cw to accommodate the sign bit. For instance, a coefficient in [10 8] format would be arranged as follows:



 The design is supplied with Matlab® scripts for the easy generation of different coefficient sets using FDAtool®. Please see application note: app\_note\_zc002.pdf for more details.



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The standard design ships with 14-bit coefficients in [14 13] format. This coefficient set is sufficient to obtain up to 80dBs of stop band attenuation with a 48-tap half-band filter. Using coefficients with a fewer number of bits will result in a smaller design, but will also compromise filter performance<sup>2</sup>.

The number of bits in the input and output samples is controlled by the parameter dw. Inputs and outputs are signed values (their format is purely relative).

#### Sampling frequency considerations

The system clock frequency is the sampling frequency of the internal filter core. This is the same as the input sample rate. The sample rate of the output data is a function of the input sampling frequency,  $F_{\rm s}$ , and the decimation factor, N, where:

$$F_{s}(at output) = \frac{F_{s}}{N}$$
where,
$$N = 2^{\text{num\_stages}}$$

#### Filter characteristic

Each decimate-by-2 filter section is a 48-tap half-band Nyquist filter with 24-taps per phase. The magnitude response, impulse response and step response of the filter are shown in Figures 2, 3 and 4.



Figure 2: Magnitude response – 48-tap half-band Nyquist filter





Figure 3: Impulse response – 48-tap half-band Nyquist filter



Figure 4: Step-response - 48-tap half-band Nyquist filter

## **Functional Timing**

Figure 5 shows a sequence of input and output samples for a decimation factor of 2. Notice that output samples are valid every  $2^{nd}$  clock cycle. Outputs should be sampled on the rising clock-edge of *clk* when *en\_out* is active high.



Figure 5: Timing waveform - downsample by 2



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Figure 6 shows a similar sequence, but this time for a decimation factor of 4. In this case, the output samples are valid every  $4^{th}$  clock cycle.



Figure 6: Timing waveform - downsample by 4

Likewise, successive decimation factors of 8, 16, 32, etc. have similar timing waveforms with the *en\_out* signal being asserted every  $8^{th}$ ,  $16^{th}$  and  $32^{nd}$  clock cycle respectively.

## Source File Description

All source files are provided as text files coded in VHDL. The following table gives a brief description of each file. Note that all generic parameters are defined in the package 'fir\_dec\_pack.vhd'.

Source file	Description	
fir_dec_pack.vhd	Package containing all generic parameters - including coefficients	
fir_dec_mad.vhd	Multiply-add block	
fir_dec_mad_centre.vhd	Multiply-add block - centre tap	
fir_dec_mad_zero.vhd	Multiply-add block - zero coeffs	
fir_dec_rnd.vhd	Rounding block	
fir_dec_sat_vhd	Saturation block	
fir_dec_s0.vhd	Filter polyphase section 0	
fir_dec_s1.vhd	Filter polyphase section 1	
fir_dec.vhd	Decimate-by-2 filter	
fir_dec_n.vhd	Top-level component	
fir_dec_n_bench.vhd	Top-level test bench	

# Functional Testing

An example VHDL testbench is provided for use in a suitable VHDL simulator. The compilation order of the source code is the same as the source file description above.

The test provided is configured for a single decimate-by-2 filter with the generic parameter *num\_stages* set to '1'. The simulation must be run for at least 1 ms during which time the impulse response and step response of the filter is tested.

The simulation generates a text file called 'fir\_dec\_n\_out.txt' that contains the output samples captured during the course of the test. Figures 7 and 8 respectively demonstrate the impulse response and step response outputs for the given test example.



Figure 7: Impulse response (2 input samples) - testbench example



Figure 8: Step response - testbench example

## Synthesis

The files required for synthesis and the design hierarchy is shown below:

- fir\_dec\_pack.vhd
  - fir\_dec\_n.vhd
  - O fir\_dec.vhd
    - fir\_dec\_s0.vhd
    - fir\_dec\_s1.vhd
      - fir\_dec\_mad.vhd
      - fir\_dec\_mad\_centre.vhd
      - fir\_dec\_mad\_zero.vhd
    - fir\_dec\_rnd.vhd
    - fir\_dec\_sat\_vhd